# Reference Sheet for the QualityCore™ Algebra II End-of-Course Assessment

#### **Equations of a Line**

Standard Form Ax + By = C A, B, and C are constants with A and B not

Slope-Intercept Form y = mx + b both equal to zero.

 $y = mx + b (x_1, y_1) is a point.$ 

Point-Slope Form  $y - y_1 = m(x - x_1)$  m = slope b = y-intercept

#### Quadratics

Standard Form of a  $ax^2 + bx + c = 0$  a, b, and c are constants, where  $a \ne 0$ . Quadratic Equation

Quadratic Formula  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ 

#### **Conic Sections**

Circle  $(x - h)^2 + (y - k)^2 = r^2$  center (h,k) r = radius

Parabola  $y = a(x - h)^2 + k$  axis of symmetry x = h vertex (h,k) directrix  $y = k - \frac{1}{4a}$  focus  $\left(h, k + \frac{1}{4a}\right)$ 

Parabola  $x = a(y - k)^2 + h$  axis of symmetry y = k vertex (h,k) directrix  $x = h - \frac{1}{4a}$  focus  $(h + \frac{1}{4a}, k)$ 

Ellipse  $\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1$  foci  $(h \pm c, k)$  where  $c^2 = a^2 - b^2$ , center (h,k)

Ellipse  $\frac{(y-k)^2}{a^2} + \frac{(x-h)^2}{b^2} = 1$  foci  $(h, k \pm c)$  where  $c^2 = a^2 - b^2$ , center (h,k)

Hyperbola  $\frac{(x-h)^2}{a^2} - \frac{(y-k)^2}{b^2} = 1$  foci  $(h \pm c, k)$  where  $c^2 = a^2 + b^2$ , center (h,k)

Hyperbola  $\frac{(y-k)^2}{a^2} - \frac{(x-h)^2}{b^2} = 1$  foci  $(h, k \pm c)$  where  $c^2 = a^2 + b^2$ , center (h,k)

### **Lines and Points**

Slope  $m = \frac{y_2 - y_1}{x_2 - x_1}$   $(x_1, y_1)$  and  $(x_2, y_2)$  are 2 points.

Midpoint  $M = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$  M = midpoint d = distance

Distance  $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ 

### Miscellaneous

Simple Interest 
$$I = prt$$
  $r = \text{rate}$   $t = \text{time}$ 

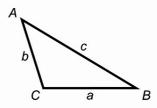
Compound Interest 
$$A = p \left(1 + \frac{r}{n}\right)^{nt}$$
  $I = \text{interest}$   $p = \text{principal}$ 

Pythagorean Theorem 
$$a^2 + b^2 = c^2$$
 a and  $b = legs$  of right triangle  $c = hypotenuse$ 

## **Laws of Sines and Cosines**

Law of Sines 
$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$

Law of Cosines 
$$a^2 = b^2 + c^2 - 2bc \cos A$$



### Sequences, Series, and Counting

Arithmetic Sequence 
$$a_n = a_1 + (n-1)d$$
  $a_n = n^{th}$  term

Arithmetic Series 
$$s_n = \frac{n}{2}(a_1 + a_n)$$
  $n = \text{number of the term}$   $d = \text{common difference}$ 

Geometric Sequence 
$$a_n = a_1(r^{n-1})$$
  $s_n = \text{sum of the first } n \text{ terms}$ 

Geometric Series 
$$s_n = \frac{a_1 - a_1 r^n}{1 - r}$$
 where  $r \neq 1$   $r = \text{common ratio}$   $k = \text{number of objects in the set}$ 

Combinations 
$${}_{k}C_{m} = C(k,m) = \frac{k!}{(k-m)! \ m!}$$
  $m = \text{number of objects selected}$ 

Permutations 
$${}_{k}P_{m} = P(k,m) = \frac{k!}{(k-m)!}$$

### Circumference, Area, and Volume

Triangle 
$$A = \frac{1}{2}bh$$
  $A = \text{area}$ 

Parallelogram 
$$A = bh$$
  $b = base$   $h = height$ 

Trapezoid 
$$A = \frac{1}{2}(b_1 + b_2)h$$
  $r = \text{radius}$   $C = \text{circumference}$ 

Circle 
$$A = \pi r^2$$
  $d = \text{diameter}$   $C = \pi d$   $V = \text{volume}$ 

$$V = \text{volume}$$
General Prism 
$$V = Bh$$

$$B = \text{area of base}$$

General Prism 
$$V = Bn$$
  $D = area of base}$ 

$$\pi \approx 3.14$$

Right Circular Cylinder 
$$V = \pi r^2 h$$

Pyramid 
$$V = \frac{1}{3}Bh$$

Right Circular Cone 
$$V = \frac{1}{3}\pi r^2 h$$
  
Sphere  $V = \frac{4}{3}\pi r^3$